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Day 2 is Tuesday, January 15, 2013

Resume Class Drill 1 Limits

Working on row where $x = -1$

We have already found $f(-1) = 1$ because dot at $(-1, 1)$

We have discussed the fact that

When x is close to -1 but to left of -1 , y is close to 1 .
This brings up the concept of the "one-sided-limit"

Symbol

$$\lim_{x \rightarrow -1^-} f(x) = 1$$

Now consider x values close to -1 but to right of -1 .

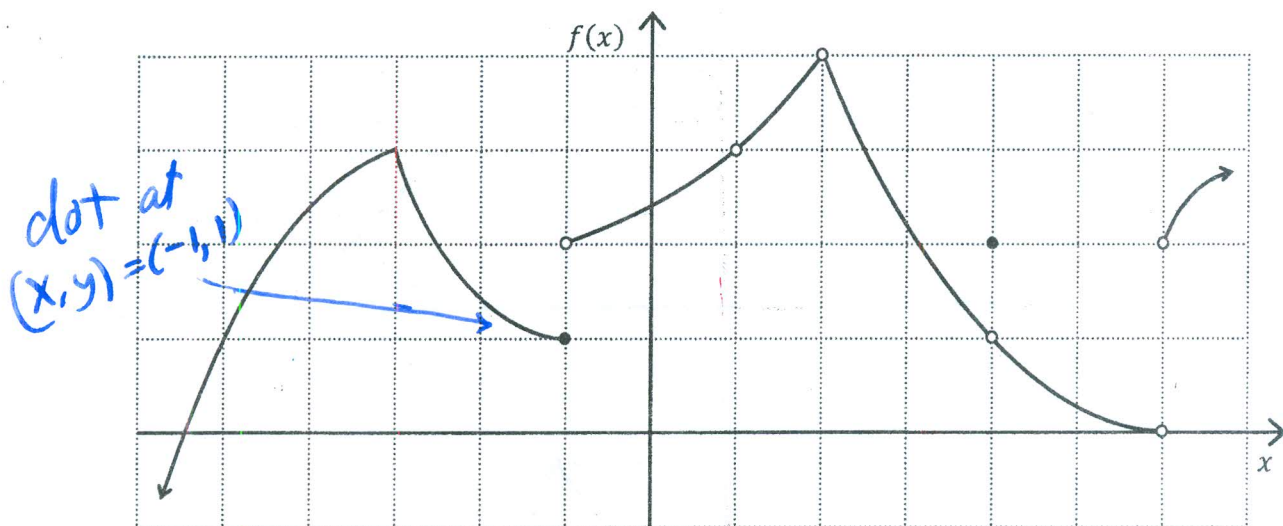
When x is close to -1 but to right of -1 , the y values are close to 2 .

Symbol:

$$\lim_{x \rightarrow -1^+} f(x) = 2$$

Class Drill 1: Limits

Use the graph to fill in the table. (Extra copies of the graph are on back.)



x-value	limit from left	limit from right	limit	y-value
-5	$\lim_{x \rightarrow -5^-} f(x) =$	$\lim_{x \rightarrow -5^+} f(x) =$	$\lim_{x \rightarrow -5} f(x) =$	$f(-5) =$
-3	$\lim_{x \rightarrow -3^-} f(x) =$	$\lim_{x \rightarrow -3^+} f(x) =$	$\lim_{x \rightarrow -3} f(x) =$	$f(-3) =$
-1	$\lim_{x \rightarrow -1^-} f(x) = 1$	$\lim_{x \rightarrow -1^+} f(x) = 2$	$\lim_{x \rightarrow -1} f(x) = \text{DNE}$	$f(-1) = 1$
1	$\lim_{x \rightarrow 1^-} f(x) = 3$	$\lim_{x \rightarrow 1^+} f(x) = 3$	$\lim_{x \rightarrow 1} f(x) = 3$	$f(1) = \text{DNE}$
2	$\lim_{x \rightarrow 2^-} f(x) =$	$\lim_{x \rightarrow 2^+} f(x) =$	$\lim_{x \rightarrow 2} f(x) =$	$f(2) =$
4	$\lim_{x \rightarrow 4^-} f(x) = 1$	$\lim_{x \rightarrow 4^+} f(x) = 1$	$\lim_{x \rightarrow 4} f(x) = 1$	$f(4) = 2$
6	$\lim_{x \rightarrow 6^-} f(x) = 0$	$\lim_{x \rightarrow 6^+} f(x) = 2$	$\lim_{x \rightarrow 6} f(x) = \text{DNE}$	$f(6) = \text{DNE}$

