

1

Day 10 is Tuesday, February 5, 2013

Quiz 3 Thursday

Practice writing out solutions to Examples  
& Match Problems

You will need to show steps clearly, with proper notation.

New Rule (a combination of two rules in the book)

The Sum Rule and Constant Multiple Rule

Single ~~two~~ equation form

$$\frac{d}{dx} (a \cdot f(x) + b \cdot g(x)) = a \cdot \frac{df(x)}{dx} + b \cdot \frac{dg(x)}{dx}$$

Diagram illustrating the derivative of a sum of functions with constant multiples:

- Red arrows point from the constants  $a$  and  $b$  to the text "constant multiple".
- Red arrows point from the functions  $f(x)$  and  $g(x)$  to the text "function".

the ~~are~~ constant multiples  
come right through  
the derivative symbol  
and become constant  
multiples in front.

# Examples

#1(A) find derivative of  $f(x) = -3x^2 + 5x - 7$

Solution Notice that I write out the steps in detail

$$\frac{d}{dx} f(x) = \frac{d}{dx} \left( \textcircled{-3}x^2 + \textcircled{5}x - 7 \right)$$

identify  
constant  
multiples

$$= \textcircled{-3} \frac{dx^2}{dx} + \textcircled{5} \frac{dx}{dx} - \frac{d7}{dx}$$

Sum + constant  
multiple rule

$$= -3(2 \cdot x^{2-1}) + 5(1) - (0)$$

Power Rule
from yesterday  
power rule
from yesterday

$$f'(x) = -6x + 5$$

Notice that this agrees with the result ~~at~~ that we got last Tuesday Jan 29 in class using the definition of the derivative.

(B) Find  $x$ -coordinates of all points on graph of  $f(x) = -3x^2 + 5x - 7$  that have tangent lines with a slope of 11.

Solution

We are told that  $m = 11$ .

But  $m$  is obtained from  $f'(x)$ .

So we are being told that  $f'(x) = 11$

and we are being asked for  $x$ .

Strategy: Set  $f'(x) = 11$  and solve for  $x$ .

$$-6x + 5 = 11 \quad \text{solve for } x$$

$$-6x + 5 - 11 = 0$$

$$-6x - 6 = 0$$

$$-6x = 6$$

$$x = -1$$

