

Tuesday, October 29, 2013 (Day 37)

- Swipe your I.D.
 - Pick up your graded work.
 - Exam 3 tomorrow covers Chapter 5.
 - Bring your O.U. I.D. to the exam
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Today: Finishing Section 5-6 Optimization

Optimization Example #2 (similar to suggested Exercise 5-6#1)

Find positive numbers x, y such that

- their product is 9000
- The sum $10x + 25y$ is minimized

Solution

Step 1 Write an equation involving $x + y$ that expresses the fact that their product is 9000.

solution

$$x \cdot y = 9000 \quad \text{equation I}$$

Step 2 Write an equation involving $x + y$ that expresses the information about the sum.

Solution Let S stand for the sum $10x + 25y$.

That is

$$S = 10x + 25y \quad \text{equation II}$$

Goal is to minimize the value of S .

Step 3 We want to eliminate the variable y .

Start by solving equation I for y in terms of x .

result:

$$y = \frac{9000}{x} \quad \text{new equation I}$$

Step 3 Substitute Equation I into Equation II to eliminate y .

result
$$S = 10x + 25\left(\frac{9000}{x}\right)$$

Notice: this equation

- only involves S and x
- it is solved for S in terms of x .

So this equation gives us S as a function of the variable x .

Use function notation to say that:

$$S(x) = 10x + \frac{25(9000)}{x}$$

Our goal is to find the value of x that minimizes the value of $S(x)$.

What is the Domain?

We're told that x, y must be positive numbers.

So, the domain is all $x > 0$.

That is, the interval $(0, \infty)$

So our job is to ~~maximize~~ minimize

$$S(x) = 10x + \frac{25(9000)}{x}$$

on the interval $(0, \infty)$

Step 5 Use calculus to solve the minimization problem.

Find critical values of $S(x)$

We will need $S'(x)$

It will help to first rewrite $S(x)$ in more useful form.

$$\text{rewrite } S(x) = 10x + 25(9000)x^{-1}$$

$$\text{derivative } S'(x) = \frac{d}{dx} (10x + 25(9000)x^{-1})$$

$$= 10 + 25(9000)(-1)x^{(-2)}$$

$$S'(x) = 10 - \frac{25(9000)}{x^2}$$

