

Staple

L A S T N A M E	F I R S T N A M E

2017-2018 Spring Semester MATH 3050 Section 101 (Barsamian) Homework 1, Due Mon Jan 22, 2018

Problem:	1	2	3	4	5	6	7	8	9	Total	Rescaled
Your Score:											
Possible:	10	10	10	10	10	10	10	20	10	100	20

- Print this cover sheet and write your name on it.
- Except for Problem [9] don't write anything else on this sheet. Do your work on separate paper.
- You are encouraged to work together, but the words that you write should be your own.
- Assemble your pages in order and staple this cover sheet to the front.
- Turn in at the beginning of class on Monday, January 22, 2018. Late papers will not be accepted.

[1] (similar to suggested problems 2.1#25, 36) Use DeMorgan's laws to find the following negations.
 (a) Find the negation of statement P : *Bob is green and George is red.*
 (b) Find the negation of statement Q : $5 \leq x < 6$.

[2] (similar to suggested problem 2.1#41)
 (a) Make a truth table for the statement form $(\sim p \vee q) \vee (p \wedge \sim q)$
 (b) Is the statement form in (a) a tautology, a contradiction, or neither? Explain.

[3] (similar to suggested problem 2.2#7) Make a truth table for the statement form $\sim p \wedge q \rightarrow r$

[4] (similar to suggested problems 2.2#15 and 2.1#14,16)
 (a) Use a truth table to verify that $p \rightarrow q \equiv \sim p \vee q$
 (b) Explain why $\sim(p \rightarrow q) \equiv p \wedge \sim q$

[5] Suppose that p and q are statements such that $p \rightarrow q$ is false. Find the truth values of the following:
 (a) $\sim p \rightarrow q$ (b) $p \vee q$ (c) $q \rightarrow p$

[6] (similar to suggested problems 2.2#20, 22, 23) Consider statement S : If $x = 3$, then $x^2 = 9$.
 (a) In words, write the *contrapositive* of S .
 (b) In words, write the *converse* of S .
 (c) In words, write the *inverse* of S .
 (d) In words, write the *negation* of S .

[7] (a) Give an example of a conditional statement A such that A is true and *the converse of A* is false.
 (b) Give an example of a conditional statement B such that B is true and *the converse of B* is also true.

[8] (similar to suggested problem 2.2 # 20) Write the negation of each statement:
 (a) If the car is red then the house is blue.
 (b) If today is February 28, then tomorrow is March 1.
 (c) If n is divisible by 6, then n is divisible by 2 and n is divisible by 3.

[9] (sim to sugg prob 2.2 # 20,22,23) Let S be the conditional statement: "If Alex is a Shark then Betty is a Jet." Some of the following statements below are the converse, inverse, contrapositive, or negation of S . Indicate which by writing the appropriate word in the blanks to the right. If none, then write "none".

- (a) If Alex is not a Shark, then Betty is not a Jet. _____
- (b) If Alex is a Shark, then Betty is not a Jet. _____
- (c) If Betty is a Jet, then Alex is a Shark. _____
- (d) If Betty is not a Jet, then Alex is not a Shark. _____
- (e) Alex is a Shark and Betty is not a Jet. _____