


## MATH 2301 (Barsamian) GW09 Finding Derivatives Graphically Using a Ruler

The goal: Given the graph of $f$ on the top axes on the next page, make a graph of $f^{\prime}$ on the bottom axes.

On the graph of $f^{\prime}$, the input will be $x$ and the output will be $f^{\prime}(x)$. Remember the graphical interpretation of $f^{\prime}(x)$ :

## Definition of the Derivative

- symbol: $f^{\prime}(a)$
- graphical interpretation: $f^{\prime}(a)$ is the number that is the slope of the line tangent to the graph of $f$ at the point where $x=a$.

Part 1: Prepare the data for your graph of $f^{\prime}$ by filling out the following table.

| $x$ | what to do on the graph of $f$ | $f^{\prime}(x)$ |
| :---: | :---: | :---: |
| 0 | Draw the line tangent to the graph of $f$ at the point where $x=0$ <br> and find its slope $m$. This slope $m$ will be the value of $f^{\prime}(0)$. |  |
| 1 | Draw the line tangent to the graph of $f$ at the point where $x=1$ <br> and find its slope $m$. This slope $m$ will be the value of $f^{\prime}(1)$. |  |
| 2 | Draw the line tangent to the graph of $f$ at the point where $x=2$ <br> and find its slope $m$. This slope $m$ will be the value of $f^{\prime}(2)$. |  |
| 3 | Draw the line tangent to the graph of $f$ at the point where $x=3$ <br> and find its slope $m$. This slope $m$ will be the value of $f^{\prime}(3)$. |  |
| 4 | Draw the line tangent to the graph of $f$ at the point where $x=4$ <br> and find its slope $m$. This slope $m$ will be the value of $f^{\prime}(4)$. |  |
| 5 | Draw the line tangent to the graph of $f$ at the point where $x=5$ <br> and find its slope $m$. This slope $m$ will be the value of $f^{\prime}(5)$. |  |
| 6 | Draw the line tangent to the graph of $f$ at the point where $x=6$ <br> and find its slope $m$. This slope $m$ will be the value of $f^{\prime}(6)$. |  |
| 7 | Draw the line tangent to the graph of $f$ at the point where $x=7$ <br> and find its slope $m$. This slope $m$ will be the value of $f^{\prime}(7)$. |  |
| 8 | Draw the line tangent to the graph of $f$ at the point where $x=8$ <br> and find its slope $m$. This slope $m$ will be the value of $f^{\prime}(8)$. |  |
| 9 | Draw the line tangent to the graph of $f$ at the point where $x=9$ <br> and find its slope $m$. This slope $m$ will be the value of $f^{\prime}(9)$. |  |
| 10 | Draw the line tangent to the graph of $f$ at the point where $x=10$ <br> and find its slope $m$. This slope $m$ will be the value of $f^{\prime}(10)$. |  |

Part 2 is on the next page.


Part 2: Using the $\left(x, f^{\prime}(x)\right)$ data from your table, make a graph of $f^{\prime}$.


