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## MATH 2301 GW15: Analyzing a Polynomial

A **partition number** for a function g(x) is an x value where g(x) = 0 or g is *discontinuous* **Remark:** A function g(x) can only *change sign* at its *partition numbers*.

Let 
$$f(x) = x^3 - 3x^2 - 9x - 5 = (x+1)^2(x-5)$$

(a) Find the partition numbers for f(x).

(b) Make a sign chart for f(x).

A **critical number** for a function f(x) is an x value x = c that has these two properties:

- (1) x = c is a partition number for f'(x). That is, f'(c) = 0 or f' is discontinuous at x = c.
- (2) f is continuous at x = c.

**Remark:** A function f(x) can only have *relative extrema* at its *critical numbers*.

Let 
$$f(x) = x^3 - 3x^2 - 9x - 5 = (x+1)^2(x-5)$$

(c) Find the critical numbers for f(x).

(d) Make a sign chart for f'(x).