Graphing Strategy

General Idea: Start with simplest, least sophisticated analysis, and proceed to more sophisticated. If a step is not easy, then skip that step.

Step 1. Analyze f(x).

- Find the *y*-intercept
- Find the *x*-intercepts.
- Does the graph of f(x) have any symmetry or any periodicity?
- What is the domain of f(x)? Where is f(x) continuous?
- Determine location of any vertical asymptotes.
- Make a sign chart for *f* and use it to determine where *f* is positive, negative, or zero.
- Determine the end-behavior (Are there horizontal asymptotes? Or do the ends of the graph go up or down?) by finding $\lim_{x\to\infty} f(x)$ and $\lim_{x\to-\infty} f(x)$.

Step 2. Analyze f'(x).

- Find f'(x), factor it, and then find the partition numbers for f'(x).
- Construct a sign chart for f'(x) and use it to determine the x coordinates where graph of f
 has a horizontal tangent line, the intervals on which f is increasing and decreasing, and the
 x coordinates of all relative maxima and minima.
- Find the *y* coordinates of all relative maxima and minima.

Step 3. Analyze f''(x).

- Find f''(x), factor it, and then find the partition numbers for f''(x).
- Construct a sign chart for f''(x) and use it to determine the intervals on which f is concave up and concave down, and to find the x coordinates of all inflection points.
- Find the y coordinates of all inflection points.

Step 4: Sketch the graph of f.

- Draw any asymptotes as dotted lines, and label them with their line equations.
- Plot the axis intercepts, relative maxima and minima, and inflection points, and label them with their (x, y) coordinates.
- Using the other information from steps 1, 2, and 3, draw the graph.