

## Continuing Section 2.3: Continuity

### Subject for this video: Positive and Negative Behavior of Graphs of Functions

This is prerequisite material, but it is very important for our course so it is worth a review.

#### Homework:

**H20:** Positive and Negative Behavior of Graphs of Functions (2.3#55,85)

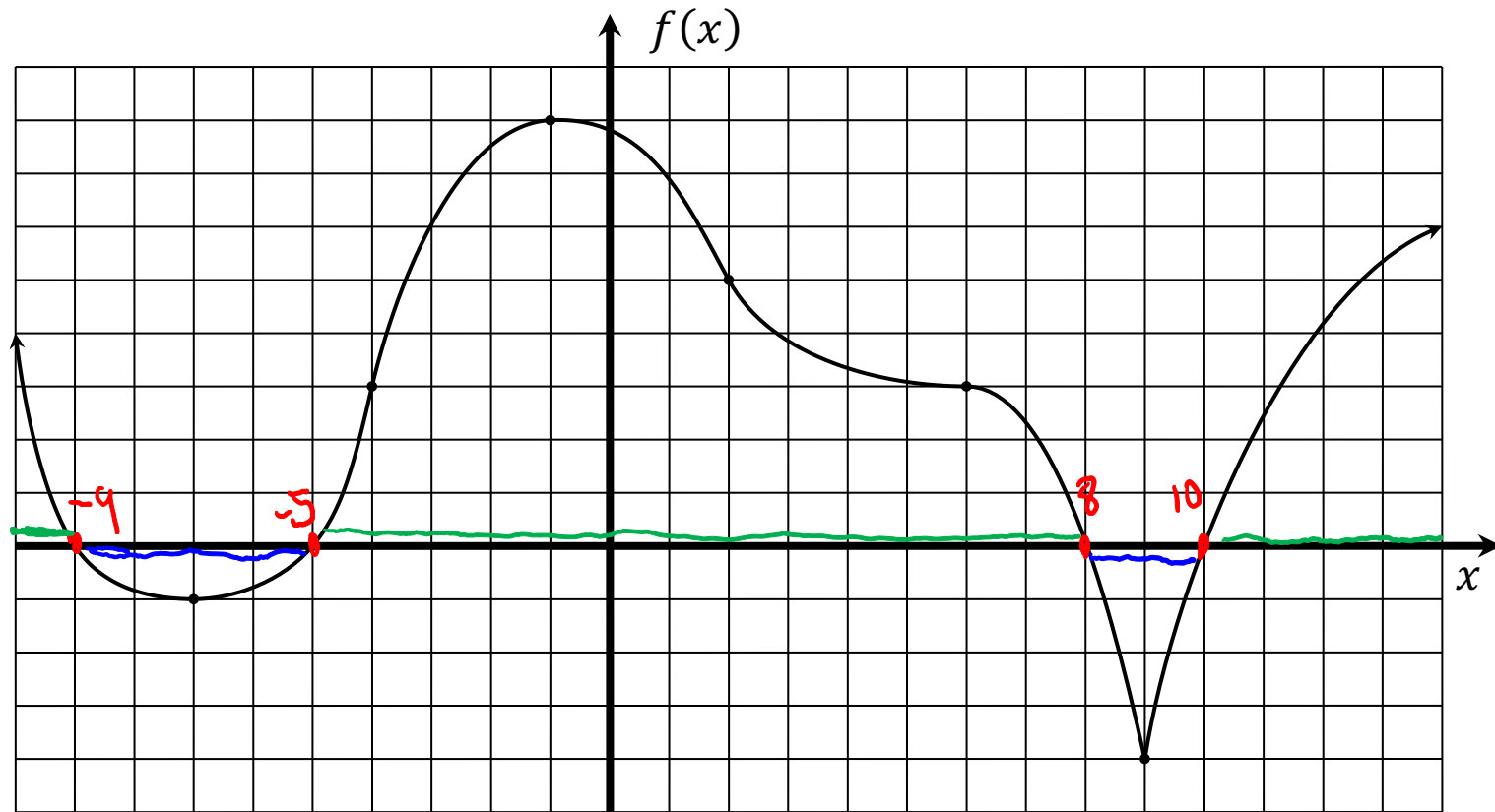
Recall definition of *positive* and *negative*.

To say a number  $y$  is positive means  $y > 0$

To say  $y$  is negative means  $y < 0$ .

(The term non-negative means  $y \geq 0$ )

[Example 1] The graph of a function  $f$  is shown below.



(1) Where is  $f(x) = 0$ ? *Where is  $y=0$ ?  $x = -9, -5, 8, 10$*

(2) Where is  $f(x) > 0$ ? Express answers in interval notation.  *$(-\infty, -9) \cup (-5, 8) \cup (10, \infty)$*   
 *$y > 0$  Graph is above the x axis*

(3) Where is  $f(x) < 0$ ? Express answers in interval notation.  *$(-9, -5) \cup (8, 10)$*   
 *$y < 0$  Graph is below the x axis.*

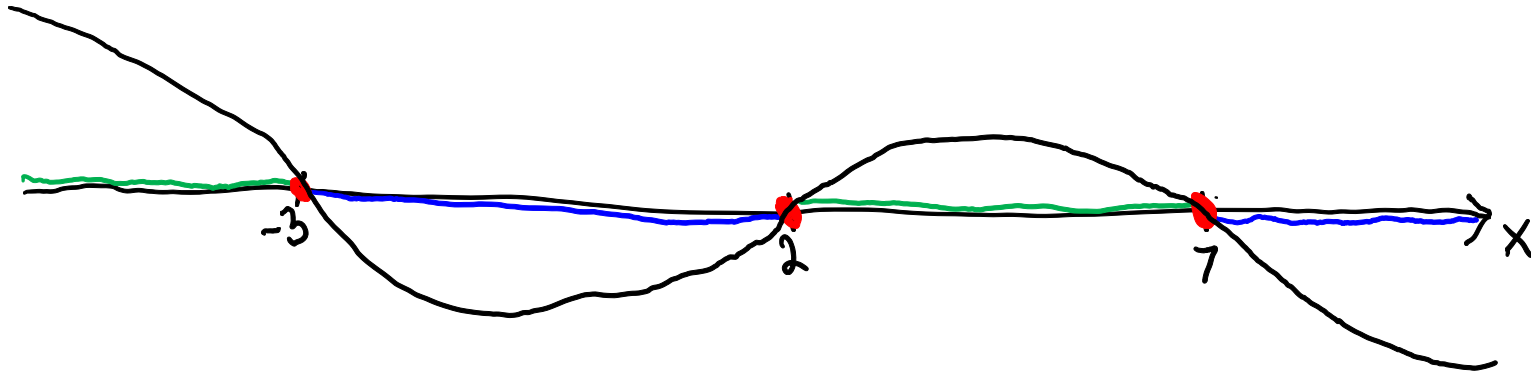
[Example 2] A function  $f(x)$  is known to have the following properties

- $f$  is continuous for all real numbers
  - $f(x) > 0$  on  $(-\infty, -3)$  and  $(2, 7)$
  - $f(x) < 0$  on  $(-3, 2)$  and  $(7, \infty)$
- x intercepts are not mentioned.*

(a) Sketch a possible graph of  $f(x)$ .

(b) Give the  $x$  coordinates of the  $x$  intercepts.

Start by indicating the positive & negative regions on a number line.



*$f$  is continuous, so the only way it can change from positive to negative is by touching the  $x$  axis and crossing it.  
So  $x$  intercepts at  $x = -3, 2, 7$*

End of Video